

Interactive parallel computation?

Any application is "parallel":

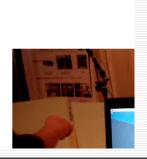
 composition of several programs / library procedures (possibly concurrent); •each procedure written independently and also possibly parallel itself.



3D-reconstruction + simulation + rendering [B Raffin &E Boyer]

- 1 monitor - 5 cameras,

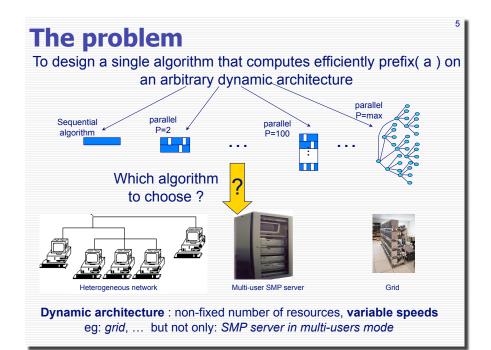
- 6 PCs

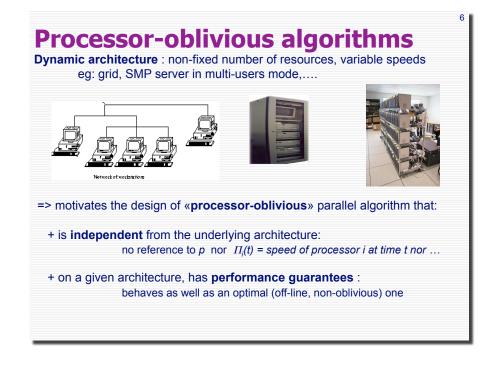


New parallel supports from small too large Parallel chips & multi-core architectures: - MPSoCs (Multi-Processor Systems-on-Chips) - GPU : graphics processors (and programmable: Shaders; Cuda SDK) - Dual Core processors (Opterons, Itanium, etc.) - Heteregoneous multi-cores : CPUs + GPUs + DSPs+ FPGAs (Cell) Commodity SMPs: 8 way PCs equipped with multi-core processors (AMD Hypertransport) + 2 GPUs Clusters: - 72% of top 500 machines - Trends: more processing units, faster networks (PCI- Express) - Heterogeneous (CPUs, GPUs, FPGAs) Grids: Heterogeneous networks - Heterogeneous administration policies - Resource Volatility Dedicated platforms: eq Virtual Reality/Visualization Clusters:

- .
- Scientific Visualization and Computational Steering
 - PC clusters + graphics cards + multiple I/O devices (cameras, 3D trackers, multi-projector displays)

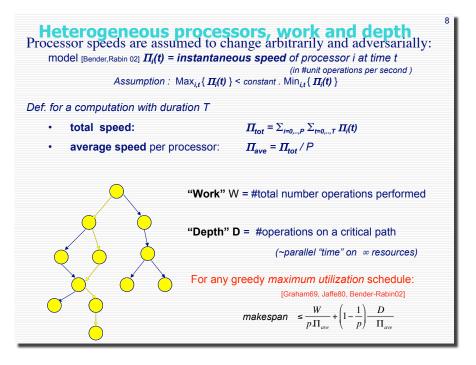


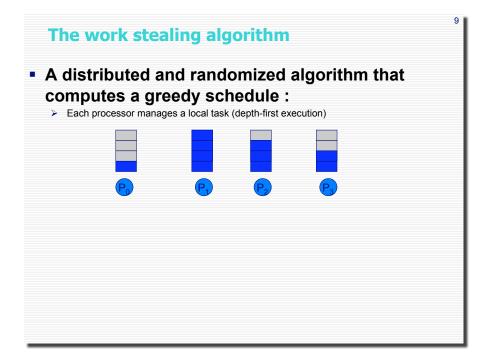




2. Machine model and work stealing

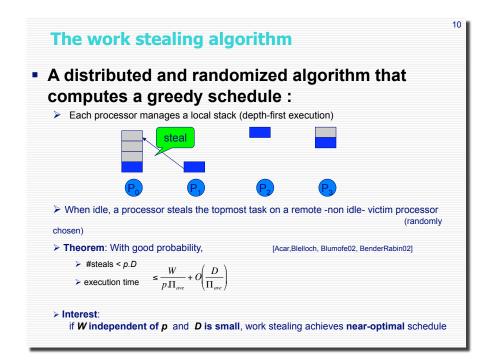
- Heterogeneous machine model and work-depth framework
- Distributed work stealing
- Work-stealing implementation : work first principle
- Examples of implementation and programs: Cilk, Kaapi/Athapascan
- Application: Nqueens on an heterogeneous grid





Proof

- Any parallel execution can be represented by a binary tree:
 - Node with 0 child = TERMINATE instruction
 End of the current thread
 - Node with 1 son = sequential instruction
 - Node with 2 sons: parallelism = instruction that
 - Creates a new (ready) thread
 - eg fork, thread_create, spawn, …
 - Unblocks a previously blocked thread
 - eg signal, unlock, send



Proof (cont)
Assume the deque implemented by an
array: each ready task stored according to
its depth in the binary tree

- On processor i at top t :
 - H_i(t) = the index of the oldest ready task

.

- Prop 1: When non zero, H_i(t) is increasing
- Prop 2: Min_(i active at t){ H_i(t) } is increasing
- Prop 3: Each steal request on i makes H_i strictly decrease.
- Corollary: if at each steal, the victim is a processor i with minimum H_i then #steals ≤ (p-1).Height(tree) ≤ (p-1).D

Proof (randomized)

- Group the steal operations in blocks of p consecutive steals:
 - After p.log p consecutive steals requests after top t, with probability > ½, any active processor at t have been victim of a steal request. [Coupon collector problem]
 - Then $\mbox{Min}_{i}\mbox{ H}_{i}$ has increased of at least 1
- In average, after 2plog p. M consecutive steals requests,

Min_i H_i has increased of M at least

- So, after 2plog p D steal requests, this is the end!
- Chernoff bounds: With high probability (w.h.p.),
 - #steal requests = O(pD log p)

Steal requests and execution time

- At each top, a processor j is
 - Either active: performs a "work" operation
 - Let wj be the number of unit work operations by j
 - Either idle: performs a steal requests
 - Let sj be the number of unit steal operations by j

Summing on all p processors :

Execution time $\leq \frac{W}{p \prod_{ave}} + O\left(\frac{D}{\prod_{ave}}\right)$

Proof (cont)

With additional hypothesis:

- Initially, only one active processor
- When several steal requests are performed on a same victim processor at the same top, only the first one is considered (others fail)

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Then #steal requests = O(p.D) w.h.p.

Remarks:

- This proof can be extended to
 - asynchronous machines (synchronization = steal)
 - Other steal policies then steal the "topmost=oldest" ready tasks, but with impact on the bounds on the steals

16 Work stealing implementation Scheduling control of the policy (close to optimal) control of the policy (realisation) Difficult in general (coarse grain) But easy if *D* is small [work-stealing] $Execution time \leq \frac{W}{p\Pi_{orc}} + O\left(\frac{D}{\Pi_{orc}}\right)$ Expensive in general (fine grain)But small overhead if a smallnumber of tasks(coarse grain)If*D*is small, a work stealing algorithm performs a small number of steals

=> Work-first principle: "scheduling overheads should be borne by the critical path of the computation" [Frigo 98]

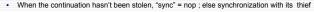
Implementation: since all tasks but a few are executed in the local stack, overhead of task creation should be as close as possible as sequential function call

At any time on any non-idle processor,

efficient local degeneration of the parallel program in a sequential execution

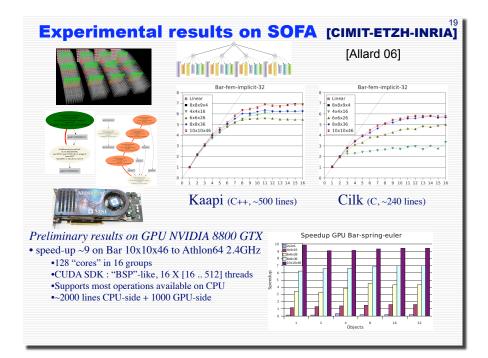
Work-stealing implementations following the work-first principle : Cilk

- Cilk-5 <u>http://supertech.csail.mit.edu/cilk/</u> : C extension
 - Spawn f (a); sync (serie-parallel programs)
 - Requires a shared-memory machine
 - Depth-first execution with synchronization (on sync) with the end of a task :
 Spawned tasks are pushed in double-ended queue
 - "Two-clone" compilation strategy [Frigo-Leiserson-Randall98] :
 on a successfull steal, a thief executes the continuation on the topmost ready task ;



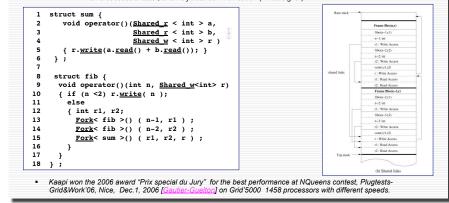
01 cilk int fib (int n)	1 int fib (int n)
02 {	3 fib_frame *f; frame pointer
03 if (n < 2) return n;	4 f = alloc(sizeof(*f)); allocate frame
. , , ,	5 f->sig = fib_sig; initialize frame
04 else	6 if (n<2) {
05 {	7 free(f, sizeof(*f)); free frame 8 return n;
	9 }
06 int x, y;	10 else {
07	11 int x, y;
<pre>08 x = <u>spawn</u> fib (n-1);</pre>	12 t ->entry = 1; save PC 13 t ->n = n; save live mars
(),	13 f->n = n; save live vars 14 *T = f; store frame pointer
09 y = <u>spawn</u> fib (n-2);	15 push(); push frame
10	16 $x = fib (n-1);$ do C call
	17 if (pop(x) == FAILURE) pop frame
11 <u>sync;</u>	18 return 0; frame stolen 19 ···· second spawn
12	20 ; second spawn sync is free!
12	20 21 free(f, sizeof(*f)); free frame
<pre>13 return (x+y);</pre>	22 return (x+v):
14 }	23 }
15 }	24 }
12 }	

 won the 2006 award "Best Combination of Elegance and Performance" at HPC Challenge Class 2, SC'06, Tampa, Nov 14 2006 [Kuszmaul] on SGI ALTIX 3700 with 128 bi-Ithanium]



Work-stealing implementations following the work-first principle : KAAPI

- Kaapi / Athapascan http://kaapi.gforge.inria.fr : C++ library
 - Fork<f>()(a, ...) with access mode to parameters (value;read;write;r/w;cw) specified in f prototype (macro dataflow programs)
 - Supports distributed and shared memory machines; heterogeneous processors
 - Depth-first (reference order) execution with synchronization on data access :
 Double-end gueue (mutual exclusion with compare-and-swap)
 - on a successful steal, one-way data communication (write&signal)



Algorithm design
From work-stealing theorem, optimizing

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- the execution time
- Find a parallel algorithm with W = Tseq and small depth
- Double criteria
 - Minimum work : W (ideally Tseq)
 - Small depth: ideally polylog in the work: = log^{O(1)} W

Algorithm design

Cascading divide & Conguer

- W(n) \leq a.W(n/K) + f(n) with a>1 - If $f(n) \ll n^{\log_{\kappa}} a \implies W(n) = O(n^{\log_{\kappa}} a)$
 - If $f(n) >> n^{\log_{\kappa}} a => W(n) = O(f(n))$
 - If $f(n) = \Theta(n^{\log_{\kappa}} a) => W(n) = O(f(n) \log n)$
- D(n) = D(n/K) + f(n)- If $f(n) = O(\log^{i} n) => D(n) = O(\log^{i+1} n)$
- D(n) = D(sart(n)) + f(n)
 - If $f(n) = O(1) => D(n) = O(\log \log n)$
 - If $f(n) = O(\log n) => D(n) = O(\log n)$

Example: Recursive and Monte Carlo computations

Competitor Competitor

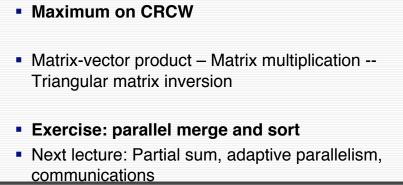
Con

 X Besseron, T. Gautier, E Gobet, &G Huard won the nov. 2008 Plugtest-Grid&Work'08 contest – Financial mathematics application (Options pricing) In 2007, the team won the Nqueens contest; Some facts [on on Grid'5000, a grid of processors of heterogeneous speeds] - NQueens(21) in 78 s on about 1000 processors - Nqueens (22) in 502.9s on 1458 processors - Naueens(23) in 4435s on 1422 processors [~24,1033 solutions] - 0.625% idle time per processor - < 20s to deploy up to 1000 processes on 1000 machines [Taktuk, Huard] - 15% of improvement of the sequential due to C++ (te during contest CPU 6 instances Nqueens(22)

> N-Queens(23 Grid'5000 fre petitor

Network



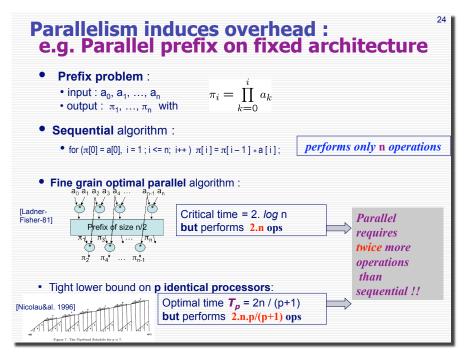


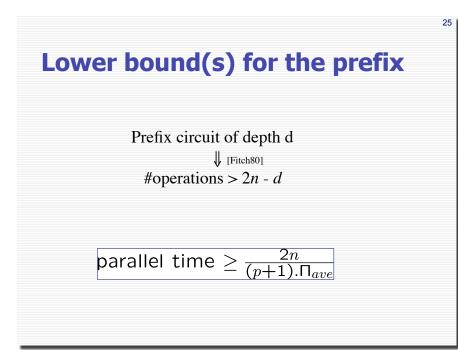
Examples

Find

Accumulate:

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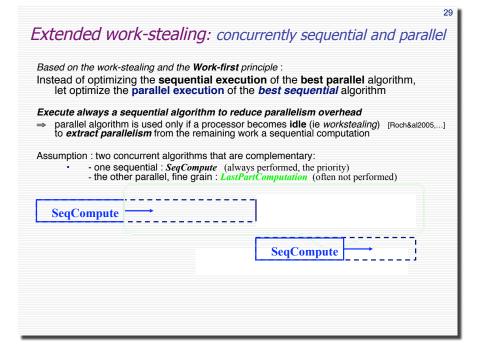


3. Work-first principle and adaptability

- Work-first principle: -implicit- dynamic choice between two executions :
 - a sequential "depth-first" execution of the parallel algorithm (local, default);
 - a parallel "breadth-first" one.
- Choice is performed at runtime, depending on resource idleness: rare event if Depth is small to Work
- WS adapts parallelism to processors with practical provable performances
 - Processors with changing speeds / load (data, user processes, system, users,
 - Addition of resources (fault-tolerance [Cilk/Porch, Kaapi, ...])
- The choice is justified only when the sequential execution of the parallel algorithm is an efficient sequential algorithm:
 - Parallel Divide&Conquer computations
 - ...
 - -> But, this may not be general in practice



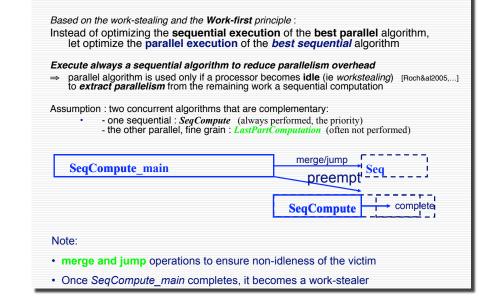
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How to get both optimal work W_1 and W_{∞} small?	
General approach: to mix both	
 a sequential algorithm with optimal work W₁ 	
- and a fine grain parallel algorithm with minimal critical time W_{ω}	
Folk technique : parallel, than sequential	
Parallel algorithm until a certain « grain »; then use the sequential one	
 Drawback : W_w increases ;o)and, also, the number of steals 	
• Work-preserving speed-up technique [BinI-Pan94] sequential, then parallel Cascading [Jajas2] : Careful interplay of both algorithms to build one with both W_{∞} small and $W_I = O(W_{seq})$	
Use the work-optimal sequential algorithm to reduce the size	
 Then use the time-optimal parallel algorithm to decrease the time 	
 Drawback : sequential at coarse grain and parallel at fine grain ;o(

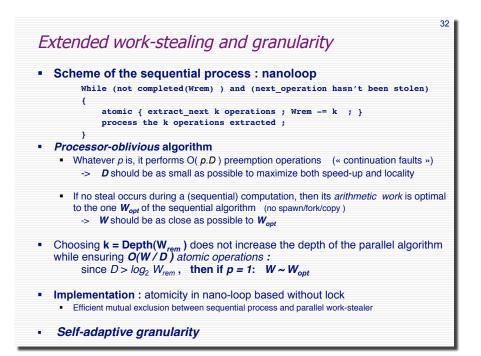




Extended work-stealing : concurrently sequential and parallel

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Interactive application with time constraint

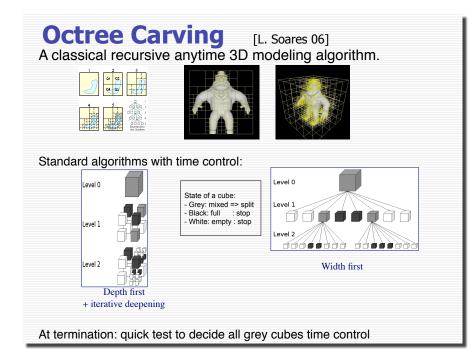
Anytime Algorithm:

- Can be stopped at any time (with a result)
- · Result quality improves as more time is allocated
- In Computer graphics, anytime algorithms are common: Level of Detail algorithms (time budget, triangle budget, etc...) Example: Progressive texture loading, triangle decimation (Google Earth)

Anytime processor-oblivious algorithm:

- On **p** processors with average speed Π_{ave} , it outputs in a fixed time **T** a result with the same quality than
- a sequential processor with speed Π_{ave} in time $p.\Pi_{ave}$.

Example: Parallel Octree computation for 3D Modeling



Parallel 3D Modeling

3D Modeling :

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build a 3D model of a scene from a set of calibrated images

On-line 3D modeling for interactions: 3D modeling from multiple video streams (30 fps)



Width first parallel octree carving

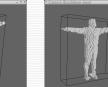
Well suited to work-stealing

- -Small critical path, while huge amount of work (eg. D = 8, W = 164 000) - non-predictable work, non predictable grain :
- For cache locality, each level is processed by a self-adaptive grain : "sequential iterative" / "parallel recursive split-half"

Octree needs to be "balanced" when stopping:

- Serially computes each level (with small overlap)
- Time deadline (30 ms) managed by signal protocol

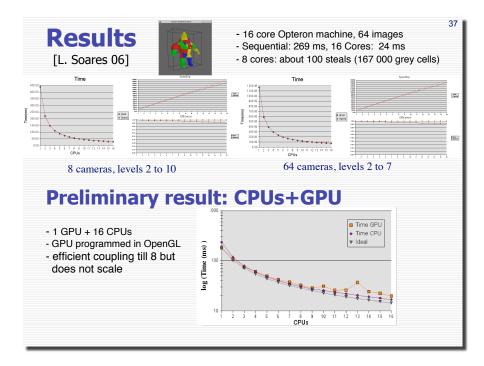






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Theorem: W.r.t the adaptive in time T on p procs., the sequential algorithm: - goes at most one level deeper : $I d_s - d_p I \le 1$; - computes at most : $n_s \le n_p + O(\log n_s)$.



4. Amortizing the arithmetic overhead of parallelism

Adaptive scheme : extract_seq/nanoloop // extract_par

- ensures an optimal number of operation on 1 processor
- but no guarantee on the work performed on p processors

Eg (C++ STL): find_if (first, last, predicate)

locates the first element in [First, Last) verifying the predicate

This may be a drawback (unneeded processor usage) :

- undesirable for a library code that may be used in a complex application, with many components
- (or not fair with other users)
- increases the time of the application :
 any parallelism that may increase the execution time should be avoided

Motivates the building of **work-optimal** parallel adaptive algorithm (**processor oblivious**)

	interactive computation, parallelism and processor oblivious of parallelism : parallel prefix
Machine mode	el and work-stealing
• Scheme 1:	Extended work-stealing : concurently sequential and parallel
• Scheme 2:	Amortizing the overhead of synchronization (Nano-loop)
• Scheme 3:	Amortizing the overhead of parallelism (Macro-loop)

4. Amortizing the arithmetic overhead of parallelism (cont'd)

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Similar to nano-loop for the sequential process :

• that balances the -atomic- local work by the depth of the remaindering one

Here, by **amortizing** the work induced by the extract_par operation, ensuring this **work to be** *small* enough :

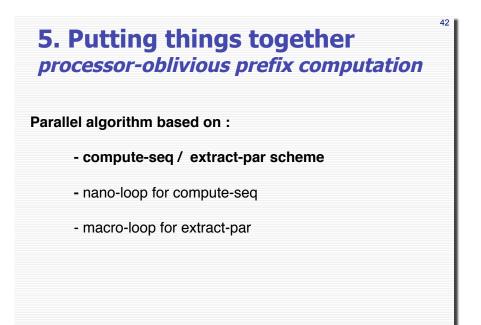
- · Either w.r.t the -useful- work already performed
- Or with respect to the useful work yet to performed (if known)
- or both.

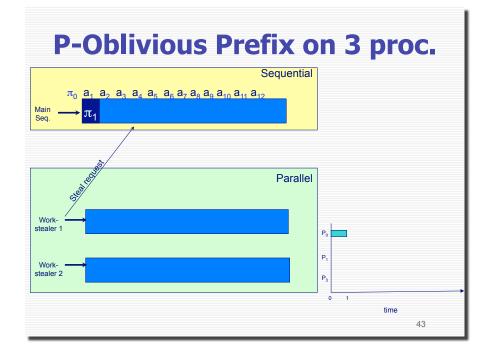
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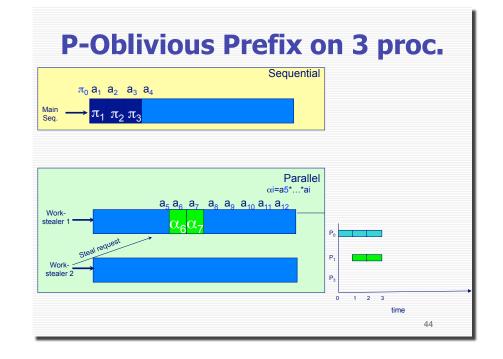
Eg : find_if (first, last, predicate) :

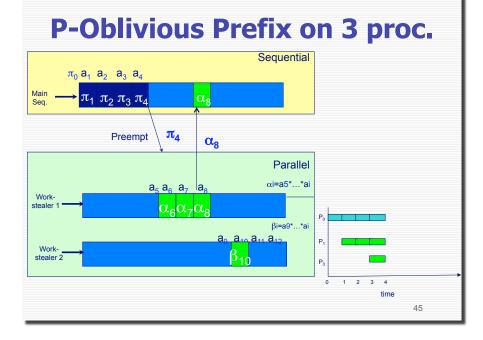
- only the work already performed is known (on-line)
- then prevent to assign more than $\alpha(W_{done})$ operations to work-stealers • Choices for $\alpha(n)$:
 - n/2 : similar to Floyd's iteration (approximation ratio = 2)
 - n/log* n : to ensure optimal usage of the work-stealers



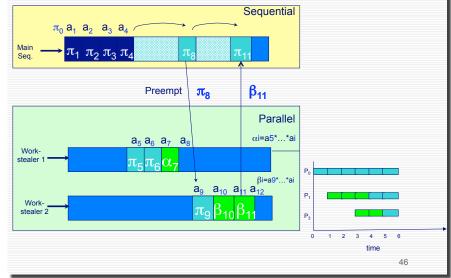


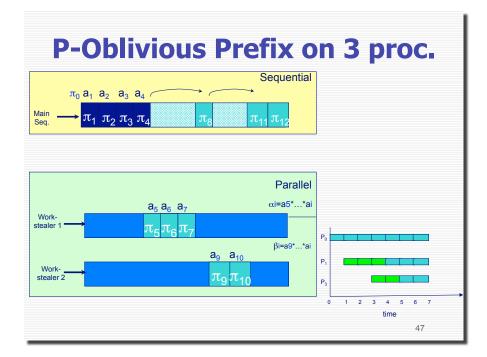


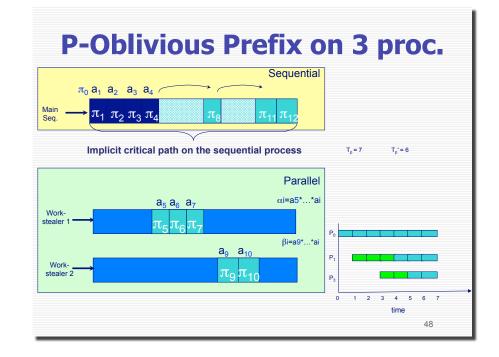


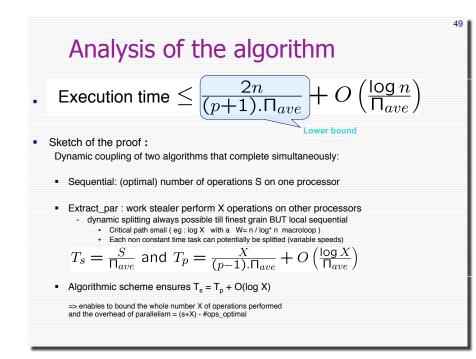


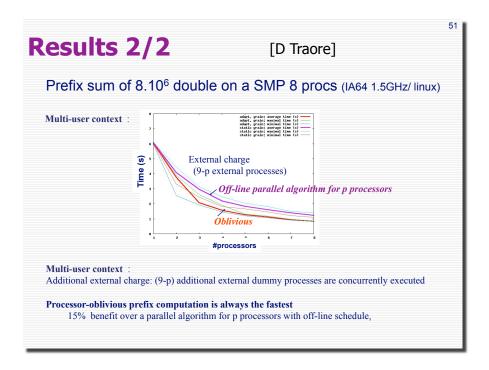


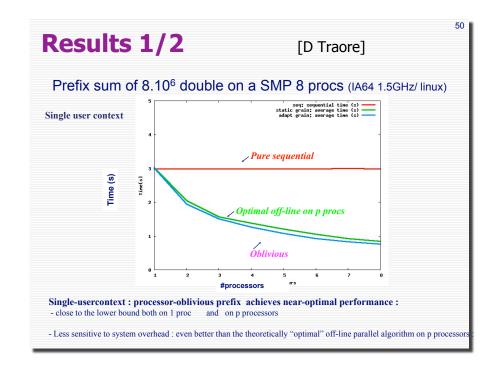




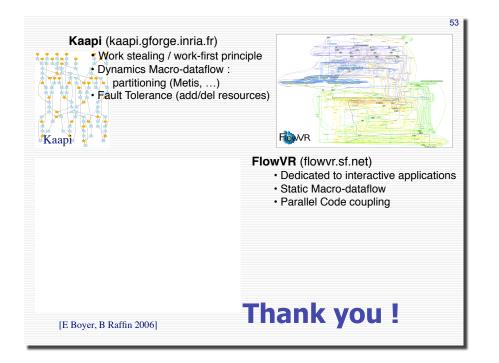




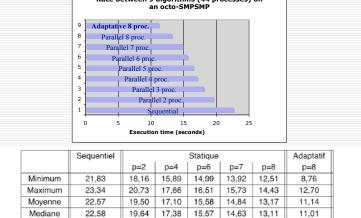




•	cessors Interest : portability ; mutualization of code ;
	Interest : portability : mutualization of code :
	Drawback : needs work-first principle => algorithm design
Effi	ciency of classical work stealing relies on <i>work-first principle</i> :
•	Implicitly defenerates a parallel algorithm into a sequential efficient ones ;
•	Assumes that parallel and sequential algorithms perform about the same amount or operations
Pro	ocessor Oblivious algorithms based on <i>WOrk-first principle</i>
•	Based on anytime extraction of parallelism from any sequential algorithm (may execute different amount of operations) ;
•	Oblivious: near-optimal whatever the execution context is.
Ger	neric scheme for stream computations :
	parallelism introduce a copy overhead from local buffers to the output



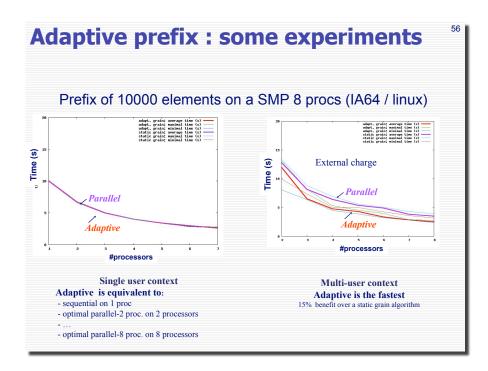


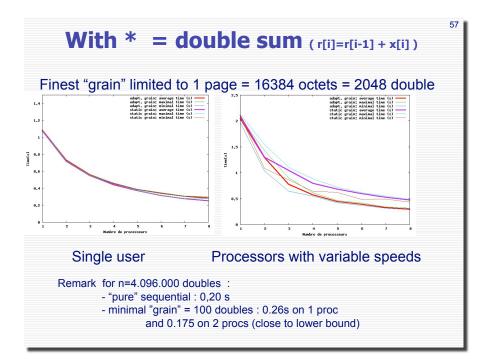


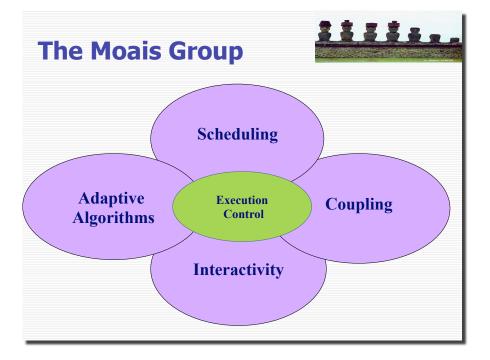
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On each of the 10 executions, adaptive completes first





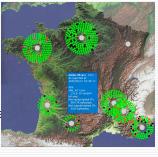




Moais Platforms

- Icluster 2 :
 - 110 dual Itanium bi-processors with Myrinet network
- GrImage ("Grappe" and Image):
 - Camera Network
 - 54 processors (dual processor cluster)
 - Dual gigabits network
 - 16 projectors display wall
- Grids:
 - Regional: Ciment
 - National: Grid5000
 - Dedicated to CS experiments
- SMPs:
 - 8-way Itanium (Bull novascale)
 - 8-way dual-core Opteron + 2 GPUs
- MPSoCs
 - Collaborations with ST Microelectronics on STE





Parallel Interactive App.

- Human in the loop
- Parallel machines (cluster) to enable large interactive applications
- Two main performance criteria:
 - Frequency (refresh rate)
 - Visualization: 30-60 Hz
 - Haptic : 1000 Hz
 - Latency (makespan for one iteration)
 - Object handling: 75 ms
- · A classical programming approach: data-flow model
 - Application = static graph
 - Edges: FIFO connections for data transfert
 - Vertices: tasks consuming and producing data
 - Source vertices: sample input signal (cameras)
 - Sink vertices: output signal (projector)
- One challenge:

Good mapping and scheduling of tasks on processors

